

## Graphing Polynomial Functions

Complete the 10-steps described in the chart for each of the following polynomial functions.

On the graph of your function, label the zeros, y-intercepts, and extrema with ordered pairs (rounded to three decimal places)

1.  $f(x) = x^4 - x^3 - 7x^2 + 13x - 6$

2.  $f(x) = -2x^3 - x^2 + 8x + 4$

3.  $f(x) = -3x^4 + 9x^3 + 3x^2 - 9x$

4.  $f(x) = 3x^4 + 7x^3 - 6x^2 - 12x + 8$

5.  $f(x) = 2x^3 - 15x^2 + 4x + 21$

6.  $f(x) = -2x^4 + 13x^3 - 21x^2 + 2x + 8$

<p>Original Function how many possible zeros (n) and extrema (n - 1) {extrema aka relative min/max}</p>	<p><b>Even</b> (reflection over y; <math>f(-x) = f(x)</math>) <b>Odd</b> (rotation 180° about origin; <math>f(-x) = -f(x)</math>) <b>Neither</b></p>
<p>End behavior:</p> <p><b>even exponent:</b> leading coefficient positive ↗ ↗ ; negative ↘ ↘</p> <p><b>odd exponent:</b> leading coefficient positive ↗ ↘ ; negative ↘ ↗</p>	<p><b>Descartes's Rule of Signs</b> (how many times the sign changes from term to term)</p> <p><math>f(x)</math>: the # of positive real zeros of f is = or less by an even amount</p> <p><math>f(-x)</math>: the # of negative real zeros of f is = or less by an even amount</p>
<p><b>Rational Zero Test</b> (p's and q's) use synthetic division—don't forget to use upper and lower bounds to help you! (if all terms have a common variable, factor it, and list it with the factors)</p>	<p>Factors and their multiplicity (even--touches x axis; odd--crosses through x-axis)</p>
<p>find the zeros</p>	<p>After graphing a sketch by hand, use a calculator to find Increasing/Decreasing Intervals</p>
<p>Extra Points including y-intercept</p>	<p><b>After graphing by hand, graph on a calculator to find</b> <b>Relative max</b> (changes from inc to dec); <b>Relative min</b> (changes from dec to inc)</p>